

# Self-Constructive High-Rate System Energy Modeling for Battery-Powered Mobile Systems

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Rice University



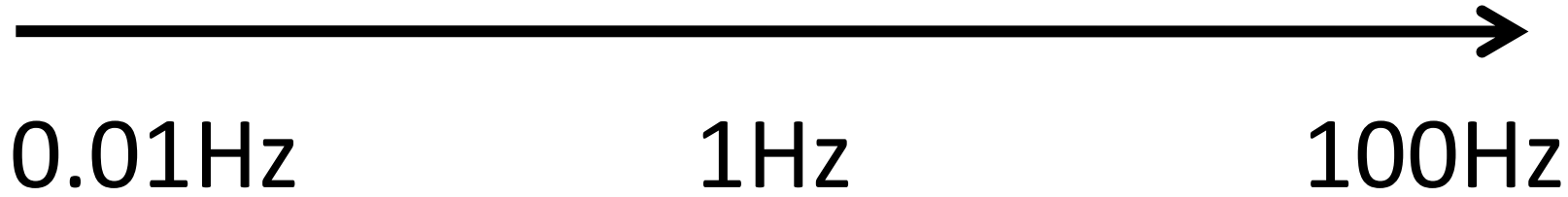
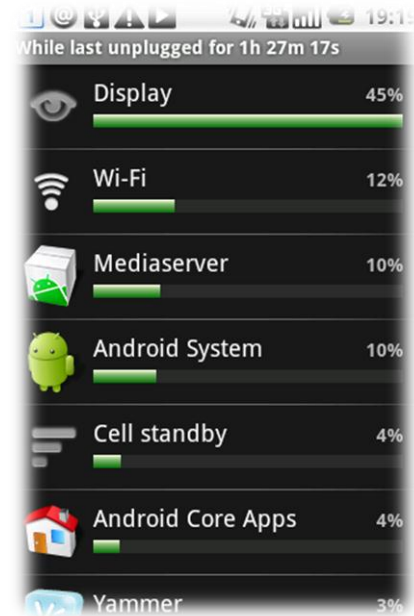
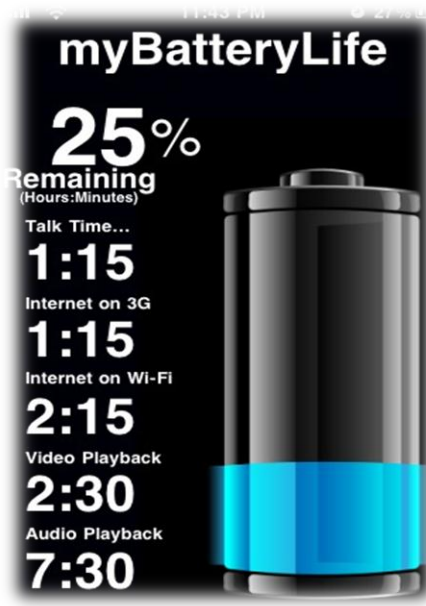
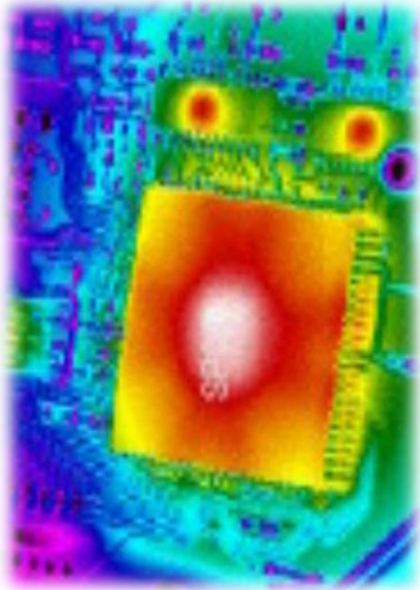
# System Energy Model

$$y(t) = f(x_1(t), x_2(t), \dots, x_p(t))$$

Response  $y(t)$ :  
Energy consumed  
by the system in  $t$

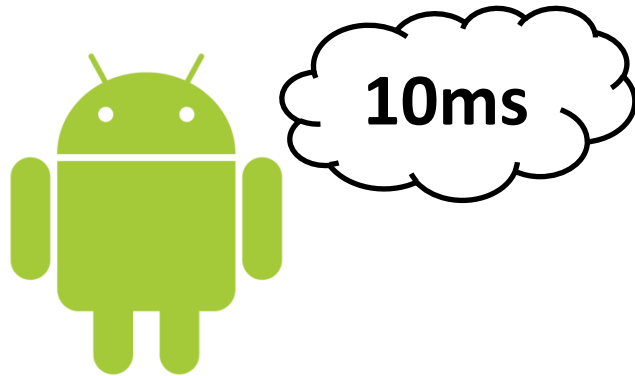
Predictors  $x_i(t)$ :  
System status  
variables in  $t$

# Rate ( $1/t$ )

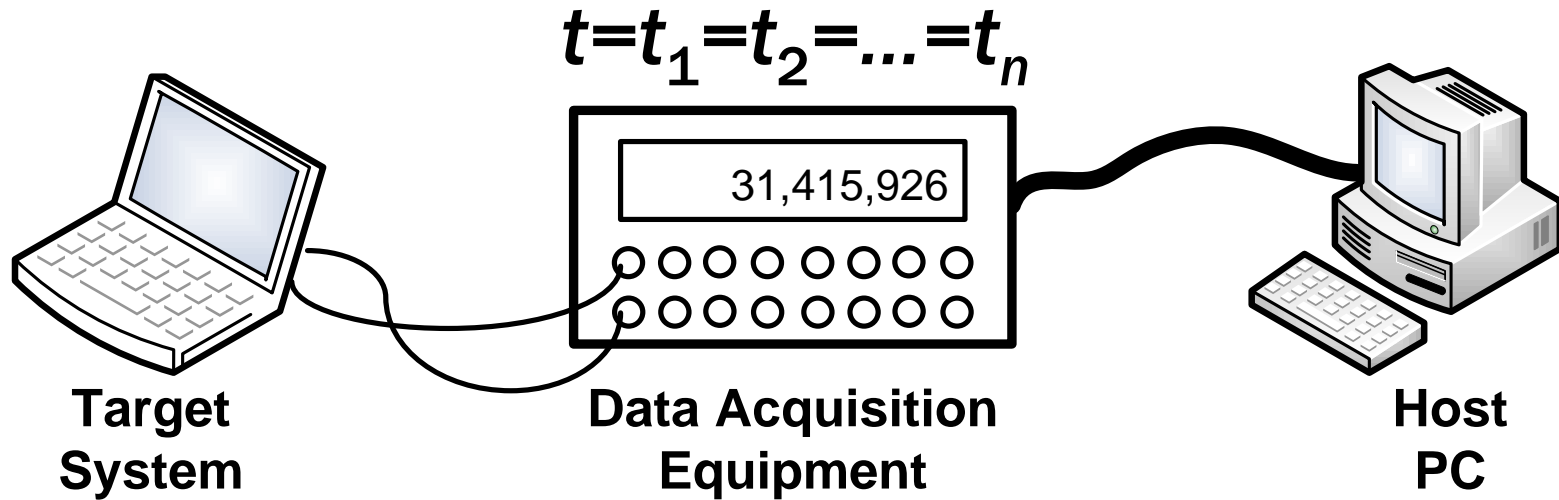


# A High-Rate Energy Model

is needed to provide an energy reading at each OS scheduling interval



# Model Construction



$$x_1(t_1) \quad x_2(t_1) \quad \dots \quad x_p(t_1)$$

$$y(t_1)$$

$$x_1(t_2) \quad x_2(t_2) \quad \dots \quad x_p(t_2)$$

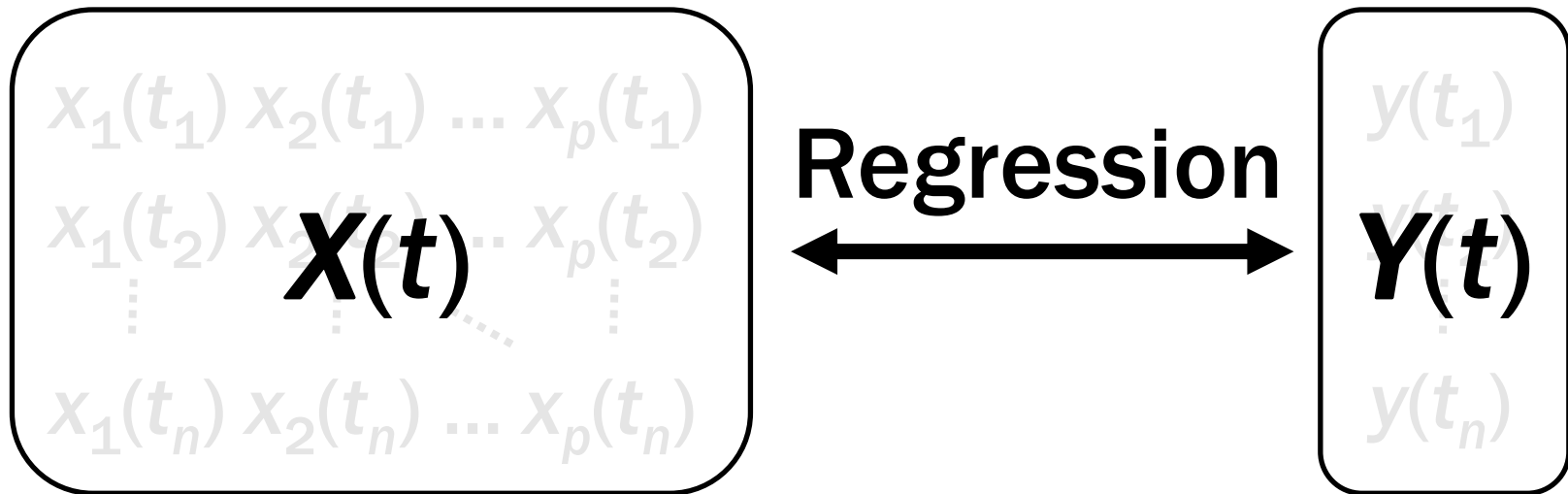
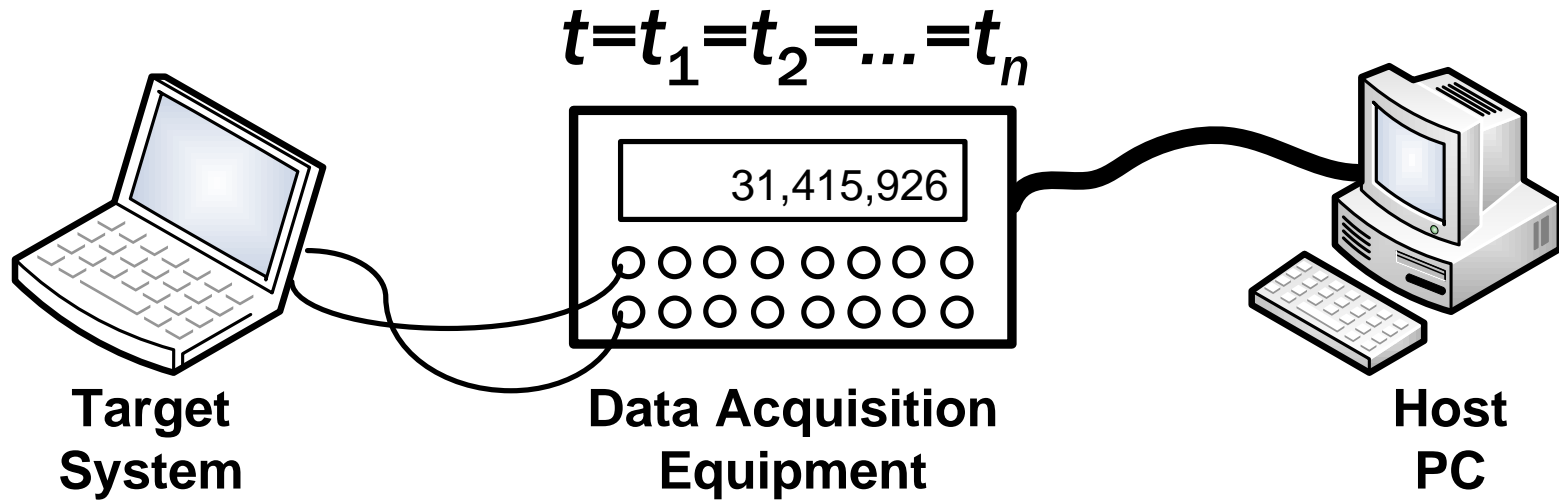
$$y(t_2)$$

$$\vdots$$
$$\vdots$$
$$\dots$$
$$\vdots$$
$$\vdots$$

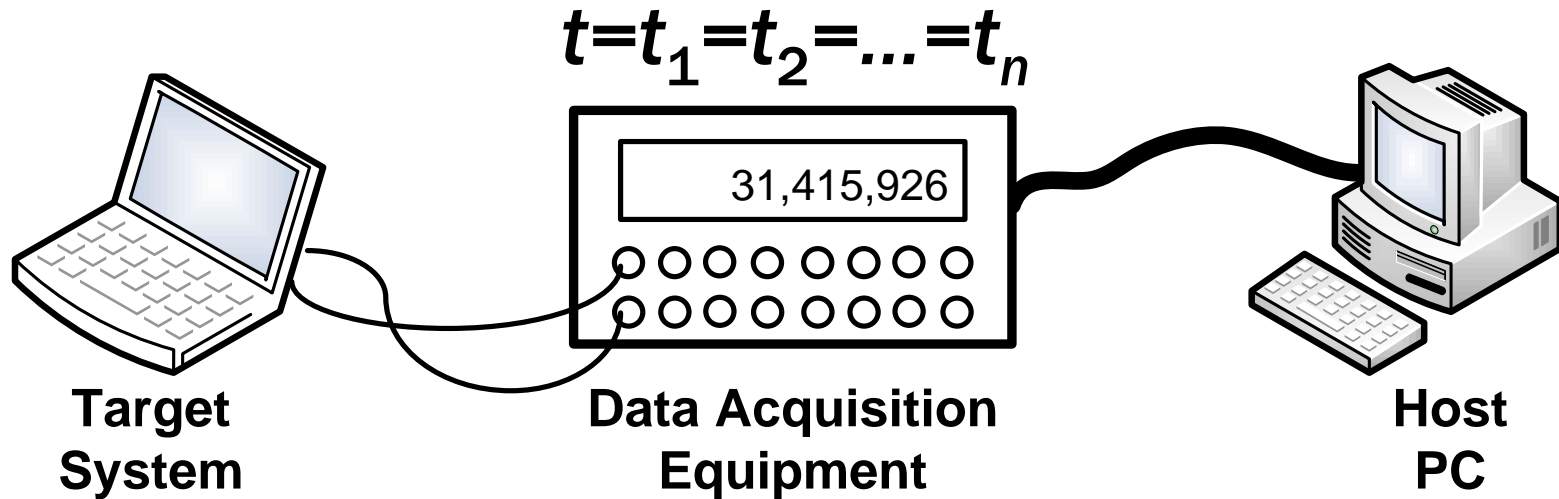
$$x_1(t_n) \quad x_2(t_n) \quad \dots \quad x_p(t_n)$$

$$y(t_n)$$

# Model Construction



# Model Construction

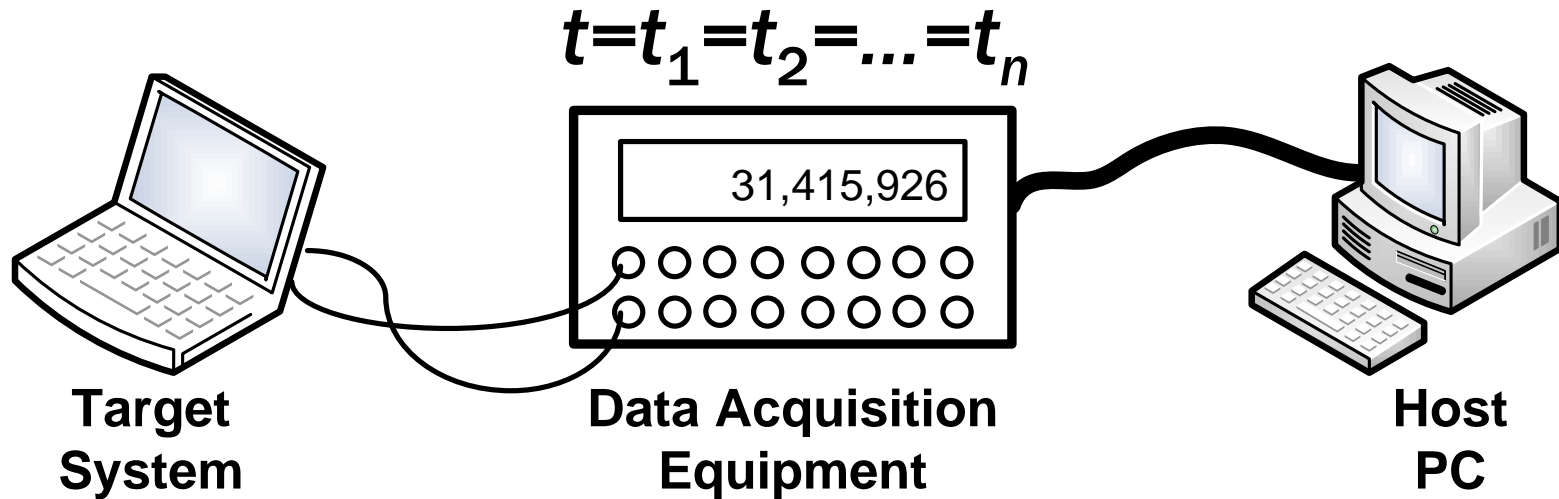


Linear Model:

$$y(t) = \beta_0 + \beta_1 x_1(t) + \dots + \beta_p x_p(t)$$

$$\hat{\beta} = \operatorname{argmin}_{\beta} (\| Y(t) - [\mathbf{1} \ X(t)] \beta \|_2)$$

# Model Construction



Linear Model:

$$\hat{y}(t) = \hat{\beta}_0 + \hat{\beta}_1 x_1(t) + \dots + \hat{\beta}_p x_p(t)$$

$$err(t_i) = \frac{\hat{y}(t_i) - y(t_i)}{y(t_i)}$$

Mean Absolute  
Root-Mean-Square

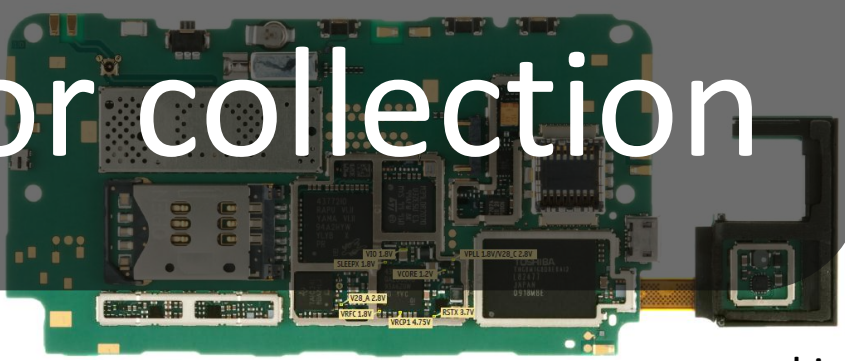
**What are the  
limitations?**

# External Devices for energy measurement

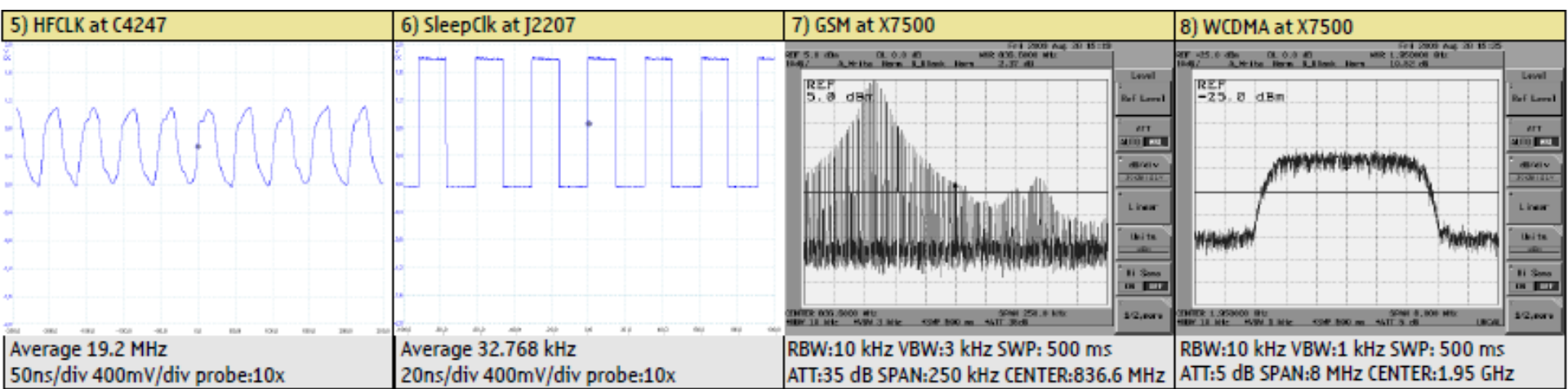




# Deep Knowledge for predictor collection




www.nokia.com





**Exclusive Model**  
for a specific platform



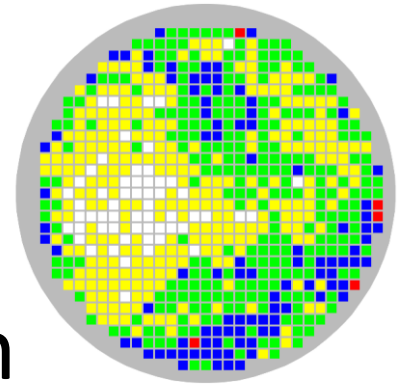
**Fixed Model** for all  
instances of the same platform



Dependencies of  
system energy models on

# **Hardware & Usage**

suggest “personalized” models  
be constructed for a mobile system





**Self-Constructive**

System Energy Modeling

**External Devices**

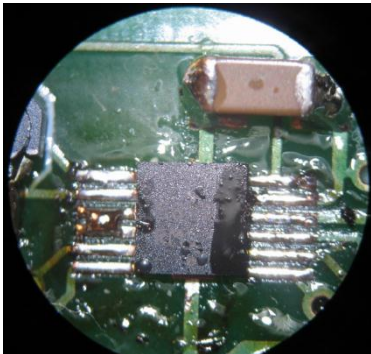
**Deep Knowledge**

**Exclusive Model**

**Fixed Model**

**Battery Interface**  
**+**  
**Statistical Learning**  
**↓**  
**Personalized**  
**Model**

# Battery Interface



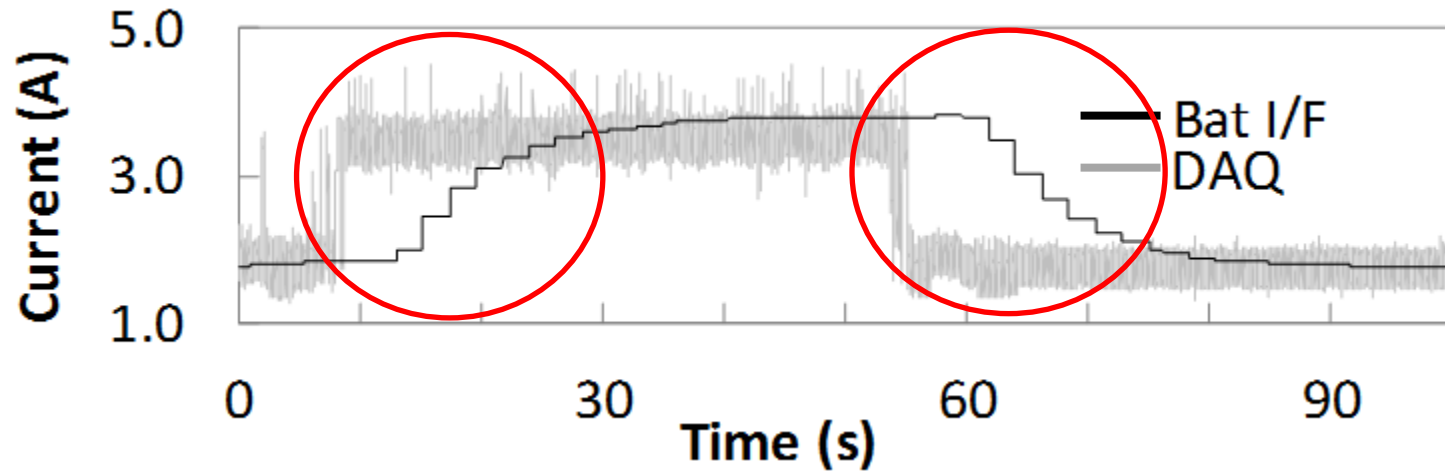
# State-of-the-art battery Interfaces are **Low-rate/Inaccurate**

	<b>N85</b>	<b>T61</b>	<b>N900</b>
<b>Max Rate</b>	4Hz	0.5Hz	0.1Hz
<b>Accuracy</b>	67%	82%	58%

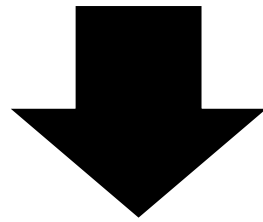
Accuracy = 100% – Root\_Mean\_Square(Instant\_Relative\_Error)

Errors in battery interface readings

are **Non-Gaussian**



Low-Rate/Inaccurate  
Battery Interface



**Statistical  
Learning**

High-Rate/Accurate  
System Energy Model

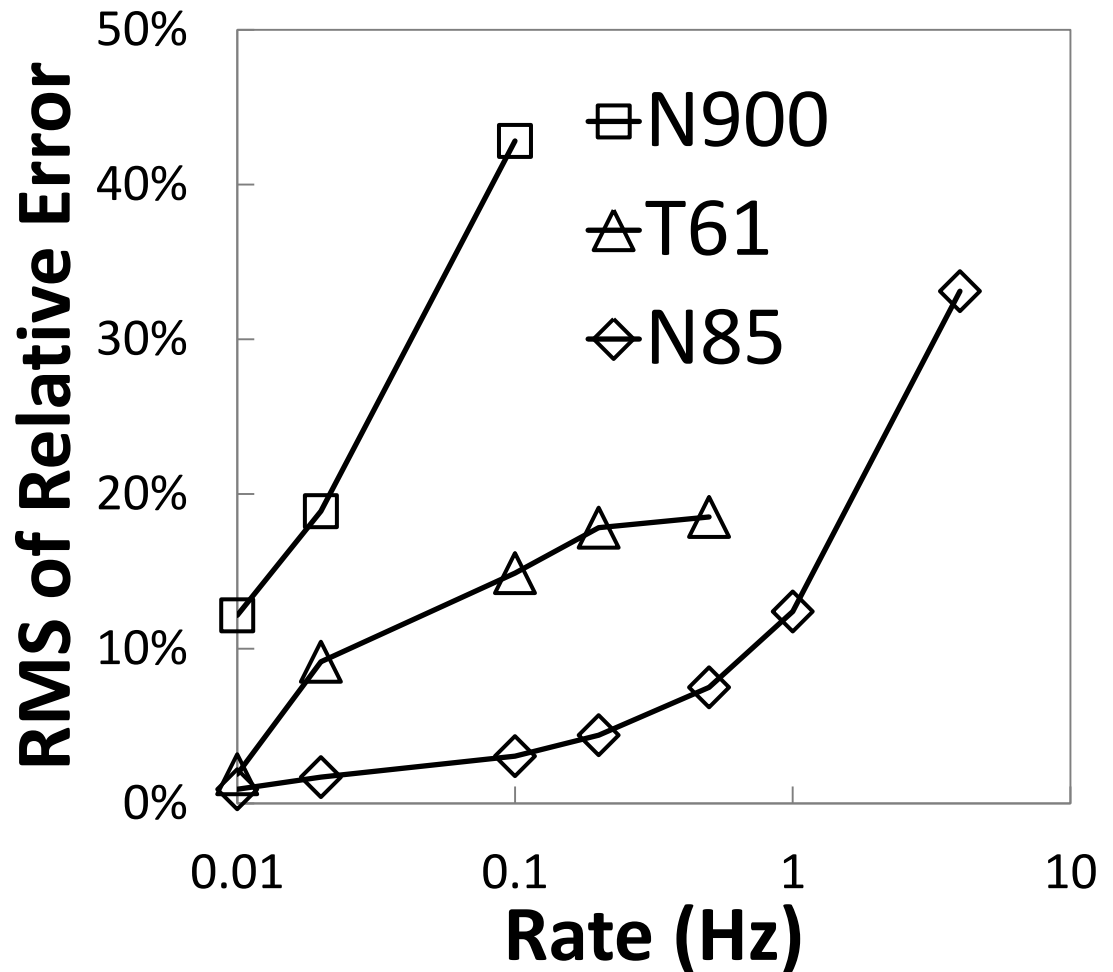
# Averaged battery interface readings

have

**Higher Accuracy**

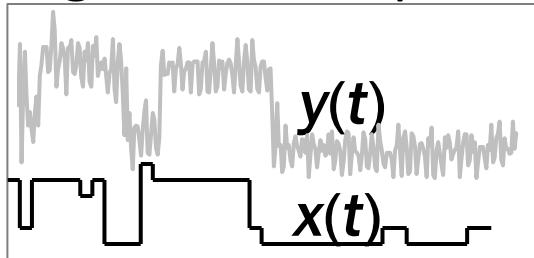
but

**Even Lower Rate**



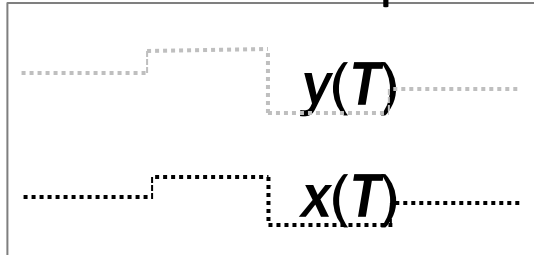
# Linear models are Independent on Time

High-rate data points

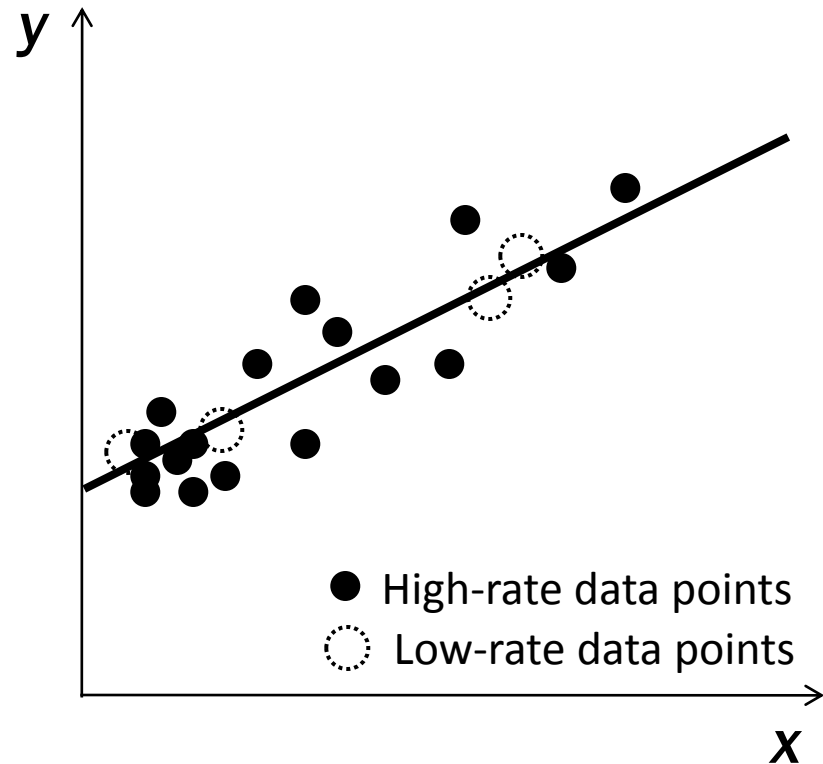


Time

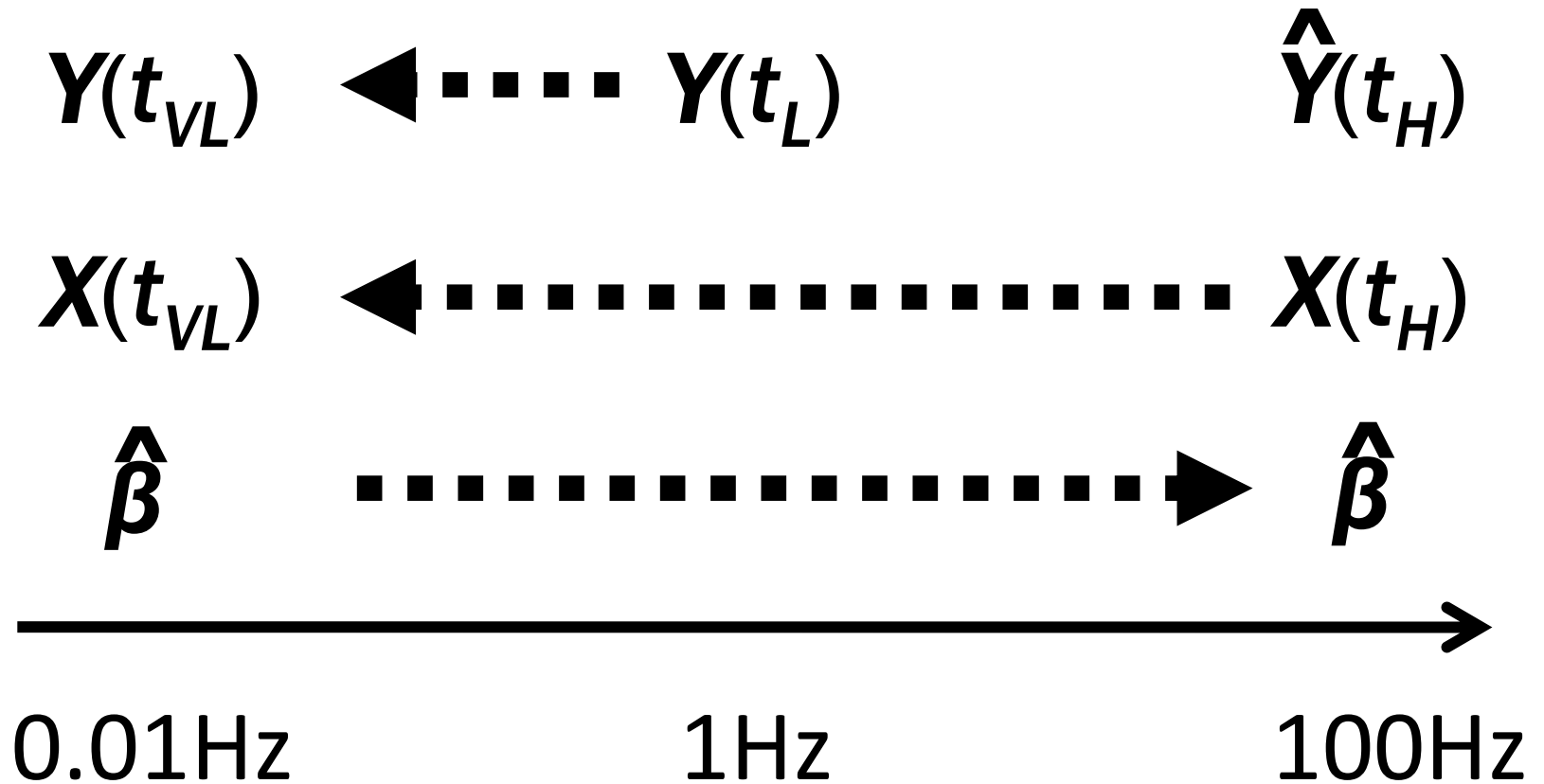
Low-rate data points

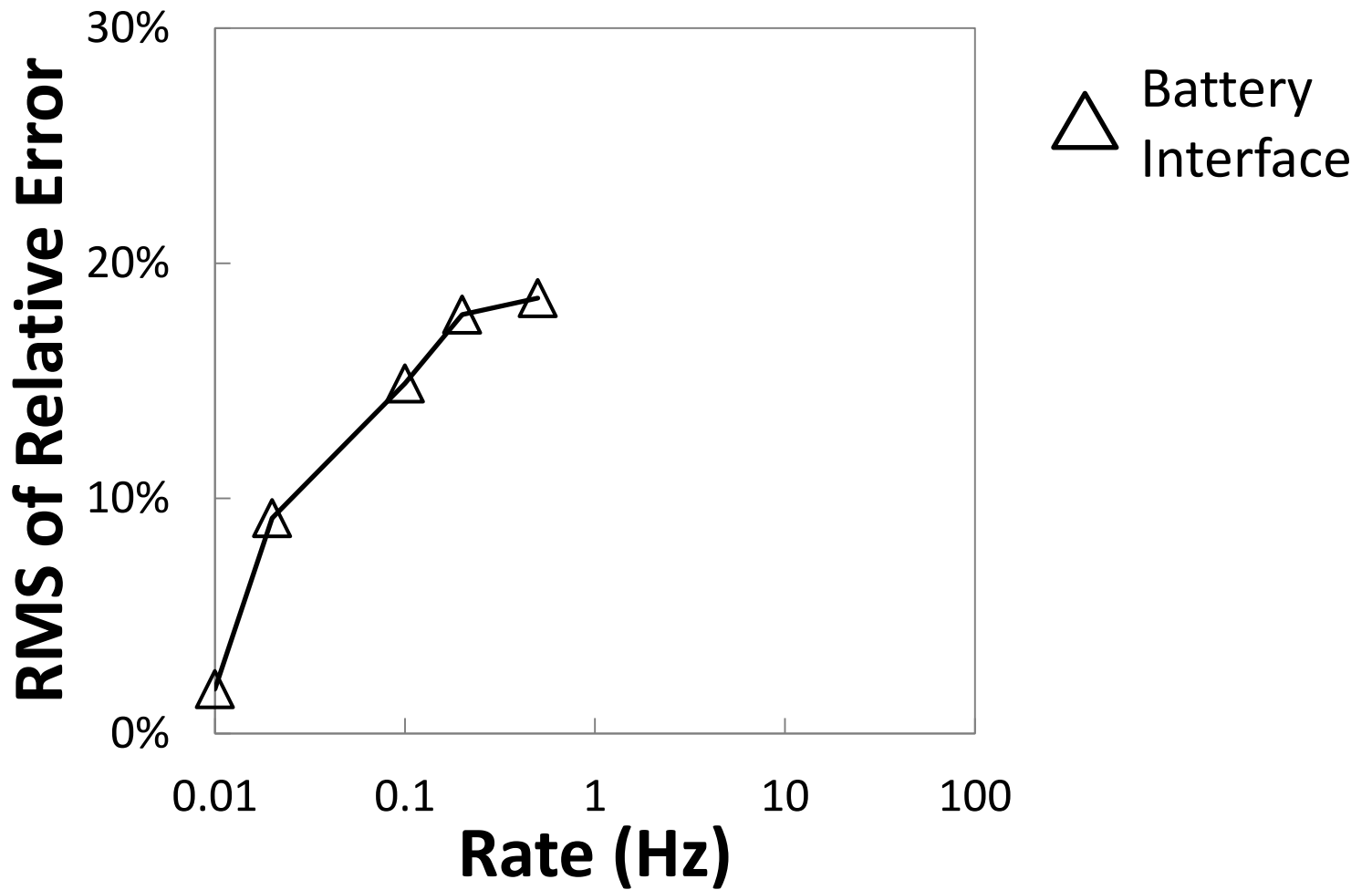


Time

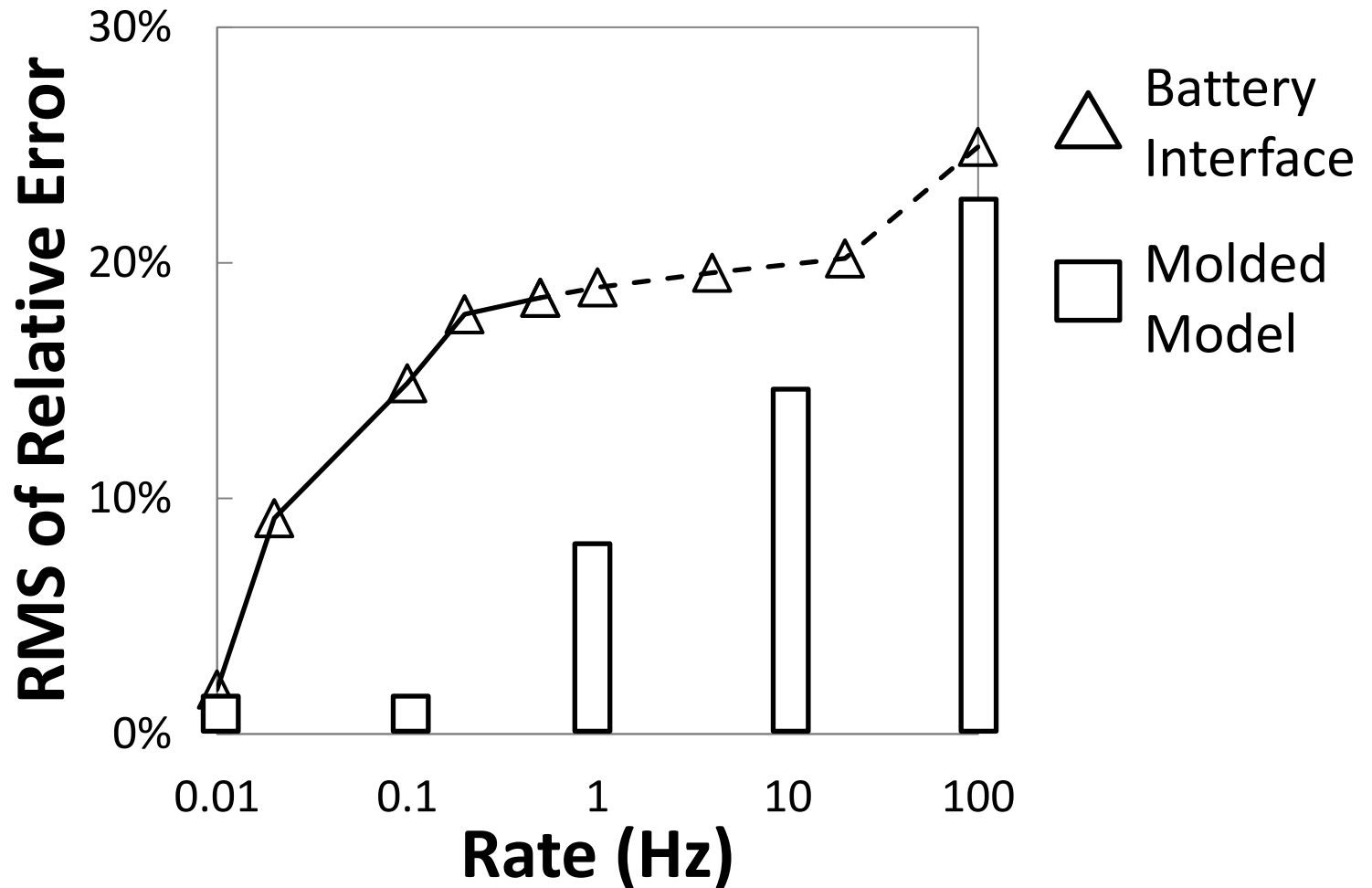


# 1. Model Molding



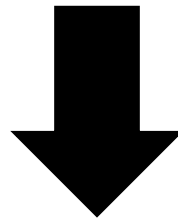


# Model Molding improves rate



# 2. Predictor Transformation

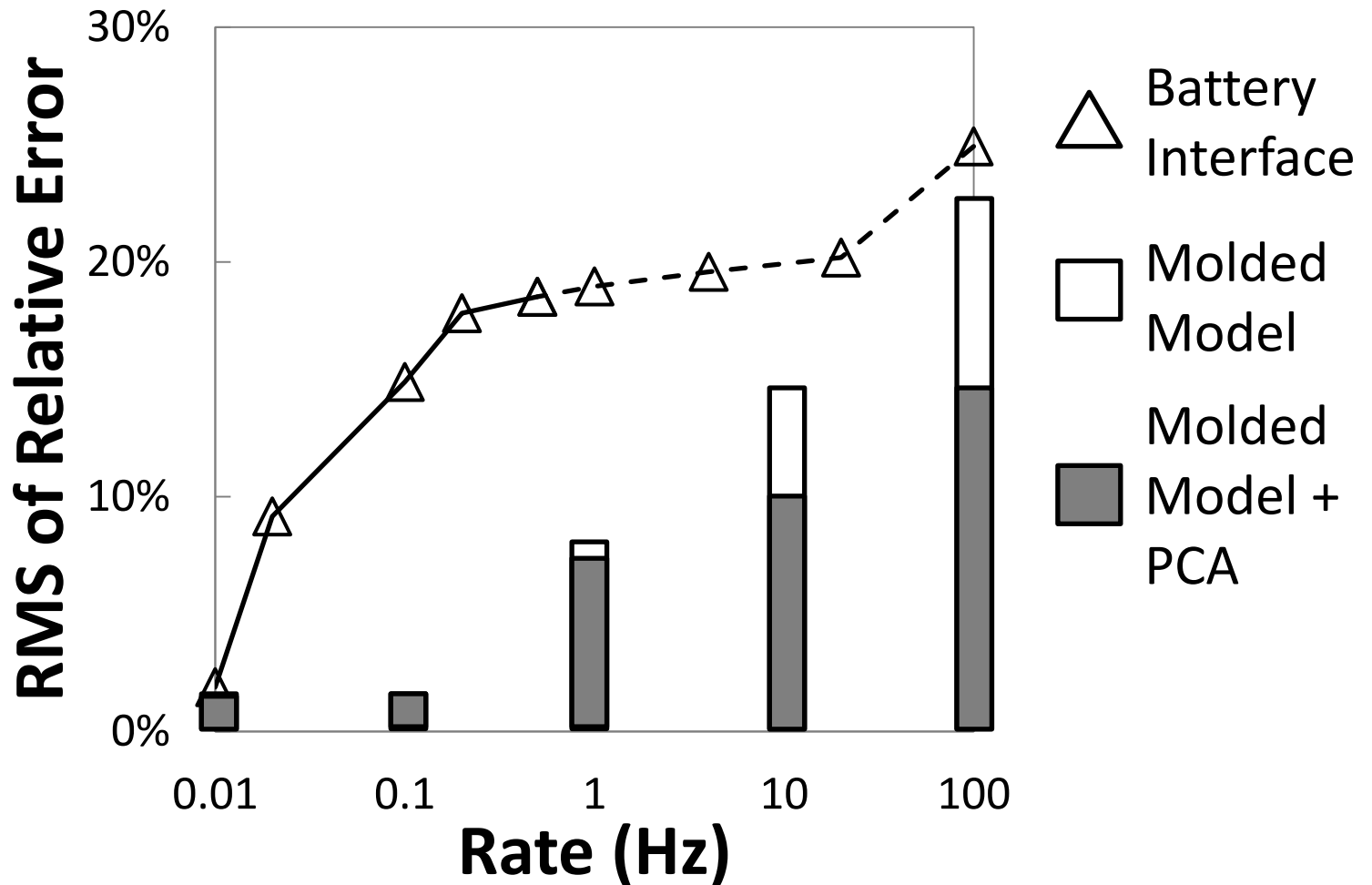
$$x_1(t), x_2(t), \dots, x_p(t)$$



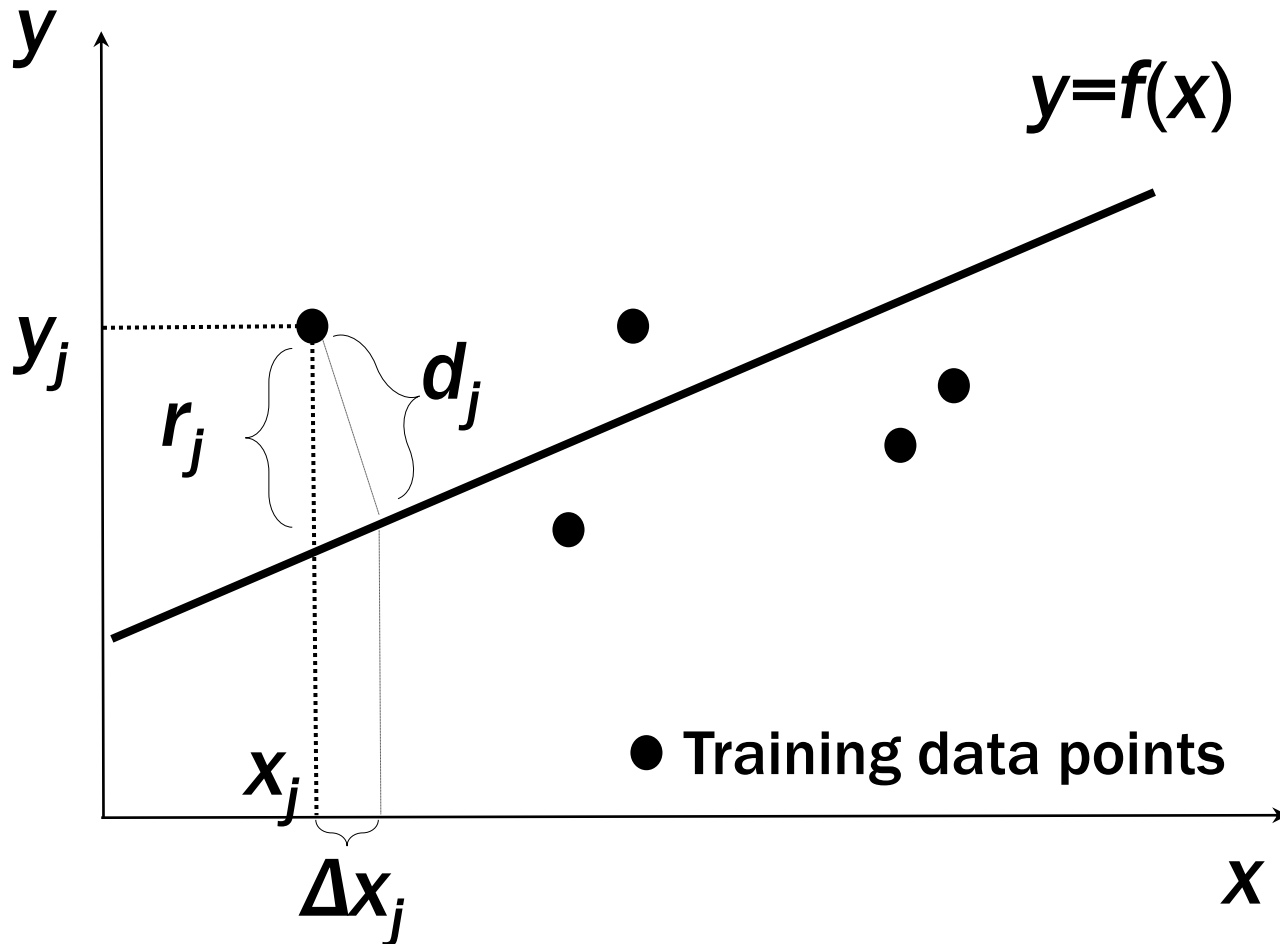
Principle  
Component  
Analysis

$$z_1(t), z_2(t), \dots, z_L(t) \quad L \leq p$$

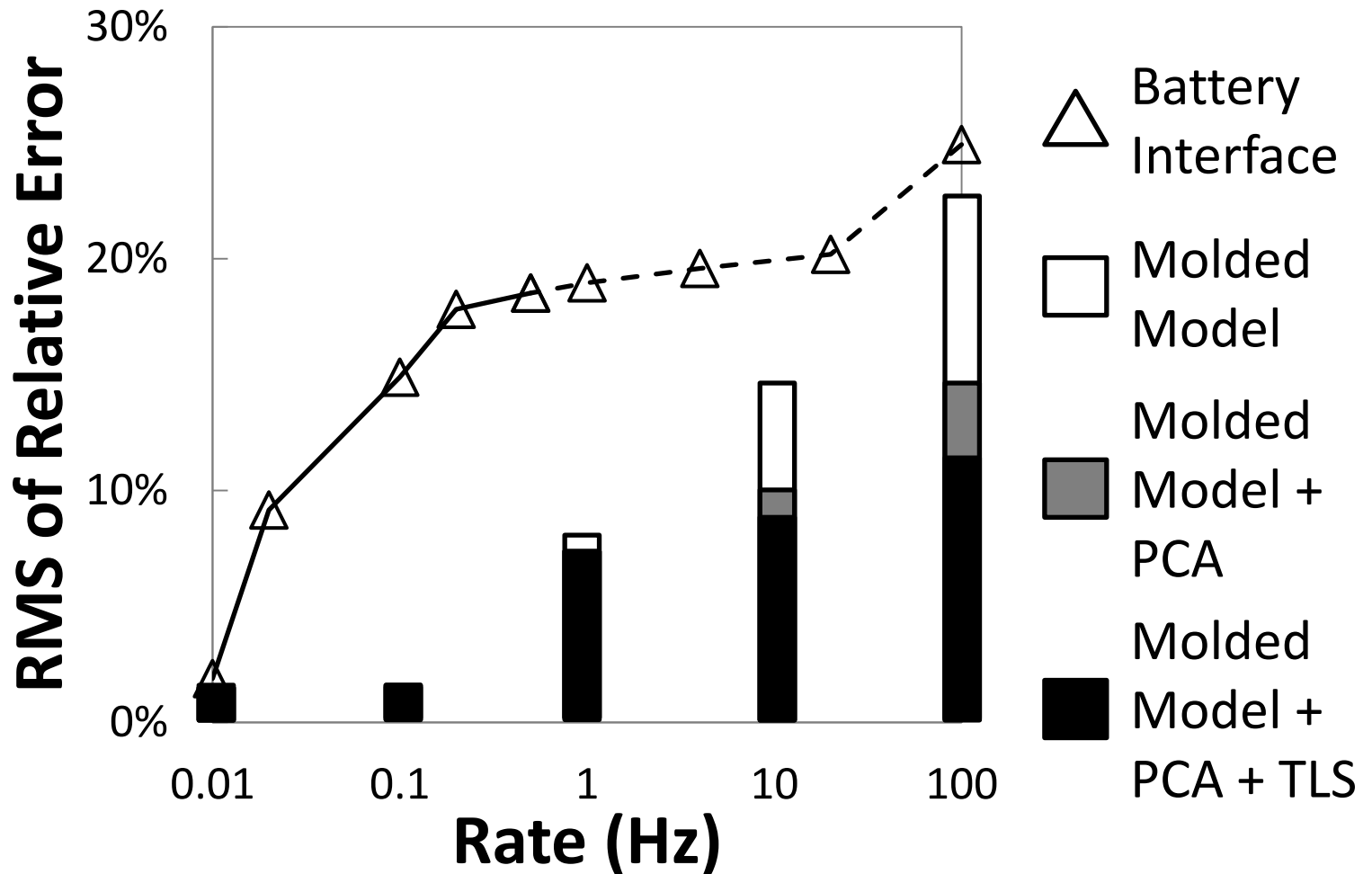
# PCA improves accuracy

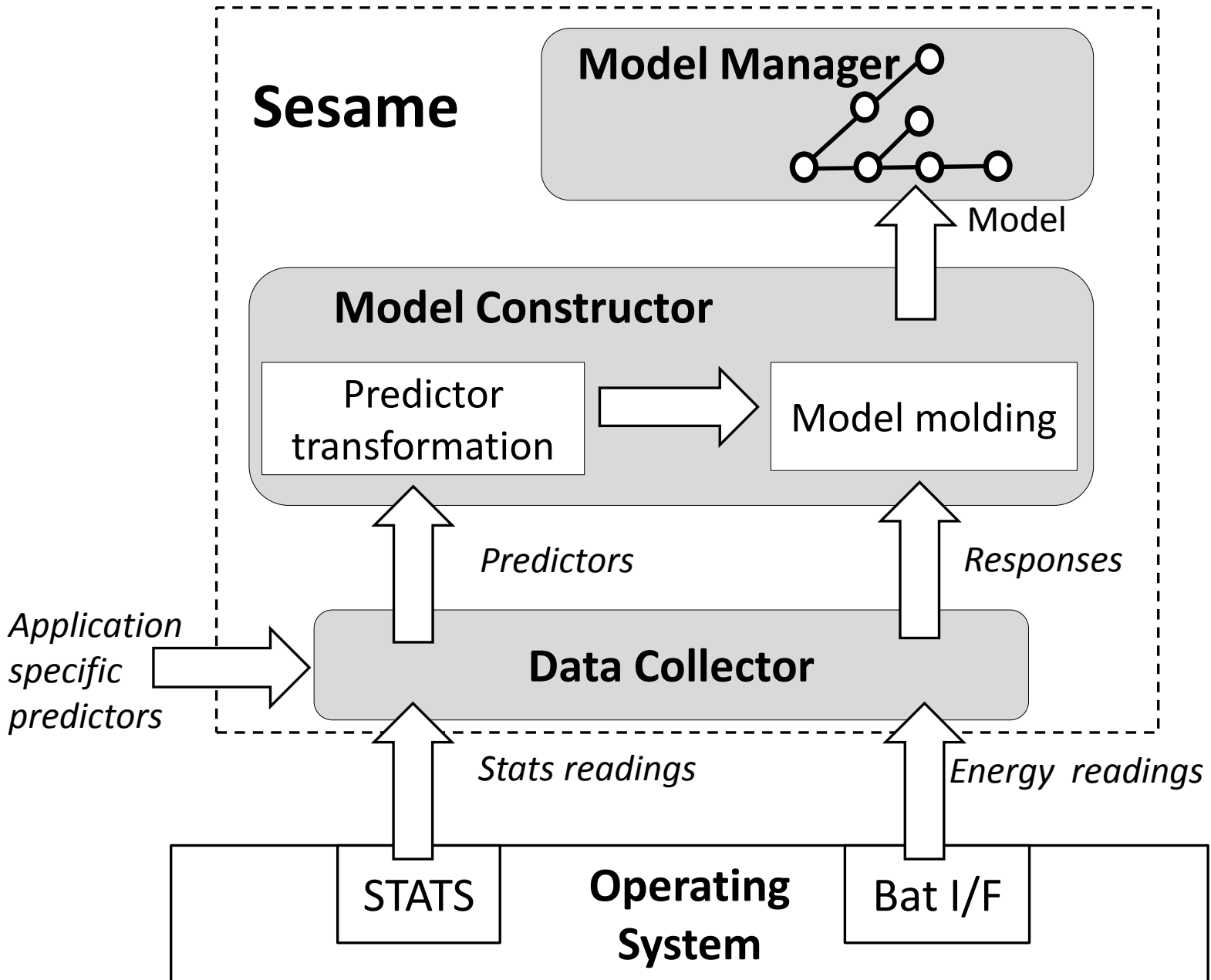


# 3. Total-Least-Square



# TLS improves accuracy at high rate





# Implementation



N900



T61

Sesame is able to generate energy models with a rate up to **100Hz**

	<b>T61</b>	<b>N900</b>
<b>1Hz</b>	95%	86%
<b>100Hz</b>	88%	82%

Accuracy = 100% – Root\_Mean\_Square(Instant\_Relative\_Error)

# Field Study



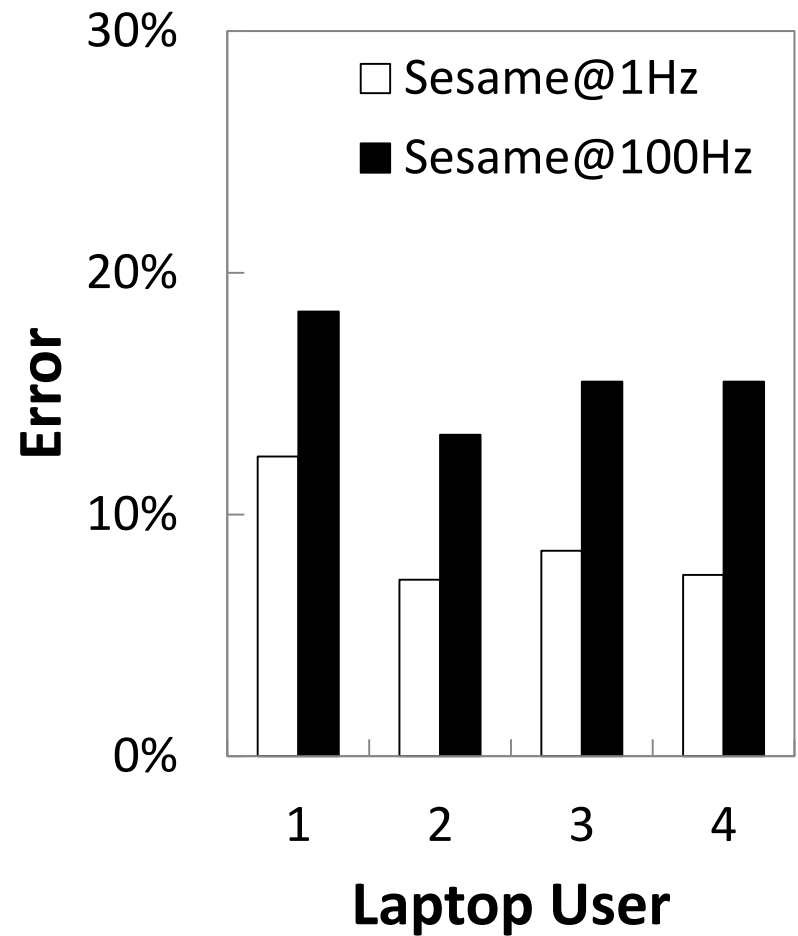
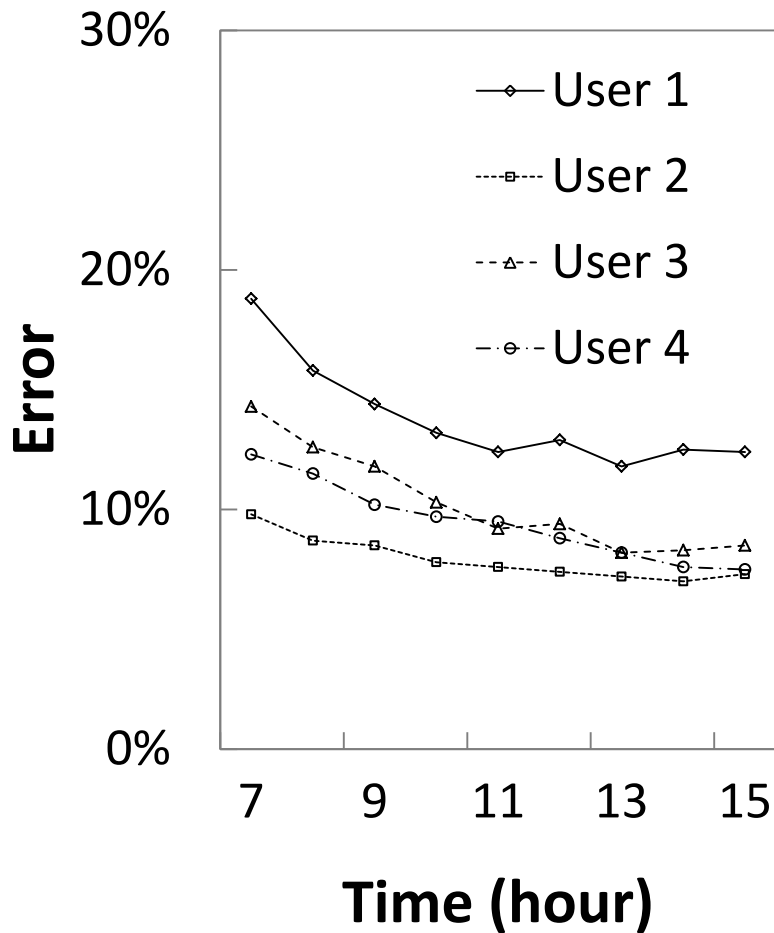
Day 1-5:  
Model Construction



Day 6:  
Model Evaluation



# Models were generated within **15** hours



Sesame is able to construct models of high accuracy because of

- 1. Sophisticated Statistical Methods**
- 2. Capability to Adapt Models**

Sesame is a high-rate/accurate  
**Virtual Power Meter**

and creates new opportunities in

**Energy Optimization  
& Management**

# Software Optimization

$$y(t) = \beta_0 + \beta_1 x_1(t) + \dots + \beta_p x_p(t)$$



“Knob”  
provided by  
target software

# Energy Accounting

$$y(t) = \beta_0 + \beta_1 x_1(t) + \dots + \beta_p x_p(t)$$

*n* Processes

# Energy Accounting

$$y(t) = \beta_0 + \beta_1 x_1(t) + \dots + \beta_p x_p(t)$$

$$x_1(t) = x_{1,1}(t) + \dots + x_{1,n}(t)$$

$$\vdots$$
$$\vdots$$
$$\vdots$$

$$x_p(t) = x_{p,1}(t) + \dots + x_{p,n}(t)$$

# Energy Contribution by Process j

$$y_j(t) = \beta_1 x_{1,j}(t) + \dots + \beta_p x_{p,j}(t)$$

Sesame can be also used for  
**Servers and Workstations**

# Conclusions

- Self-Modeling is necessary to adapt to the changes in hardware and usage
- Statistical methods help to construct high-rate /accurate models from low-rate/inaccurate battery interfaces
- Sesame creates new opportunities in system energy optimization and management